## Lecture 4

<u>**Q.</u>** Find the deflection at C of the following simply-supported beam. Length is in meter. Given:</u>

 $E= 200 \text{ GPa} = 200*10^9 \text{ Pa or N/m}^2$ 

Inertia,  $l = 400 * 10^{6} \text{ mm}^{4}$ 





Solution:

The equation we work with is  $\Delta = \int \frac{M_0 M_1}{EI} dx$ ,

Where  $M_o$  = Bending moment distribution due to actual or real loading  $M_1$  = Bending moment distribution due to virtual or unit loading E = modulus of elasticity of the material of beam I = moment of inertia of beam section L = beam span  $\Delta_c$  = deflection at point C Inertia, I = 400\*10<sup>6</sup> mm<sup>4</sup> = 400\*10<sup>6</sup> /(1000)<sup>4</sup> m<sup>4</sup> = 0.0004 m<sup>4</sup> The diagram for  $M_0$  is-



The diagram for M<sub>1</sub> is-



We know that 
$$\Delta = \int \frac{M_0 M_1}{EI} dx$$

Hence,

El 
$$\Delta_{\rm C} = \int_0^2 {}^{\mathbf{A} \to \mathbf{B}} (13.75x)(.5x)dx + \int_0^2 {}^{\mathbf{B} \to \mathbf{C}} \{13.75(x+2) - 5x\}\{0.5(x+2)\}dx + \int_0^4 {}^{\mathbf{D} \to \mathbf{C}} (31.25x - \frac{10x^2}{2})(0.5x)dx$$

$$EI.\Delta_{C} = \int_{0}^{2} {}^{A \to B} \{13.75 * x\} \{.5 * x\} dx + \int_{0}^{2} {}^{B \to C} \{13.75 * (x + 2) - 5 * x\} \{.5 * (x + 2)\} dx + \int_{0}^{4} {}^{D \to C} \{(31.25 * x) - 10x^{2}/2\} \{.5 * x\} dx$$

= 303.33

$$\Delta_{c} = \frac{303}{EI} \text{ kN. m}^{3} = \frac{303 * 1000 \text{ N.m}^{3}}{\left(200 * \frac{10^{9} \text{ N}}{m^{2}}\right) * 0.0004 \text{ m}^{4}} = 0.0038 \text{ m}}$$
$$= 3.8 \text{ mm (J)}$$

Credit: Sama Ahmed

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