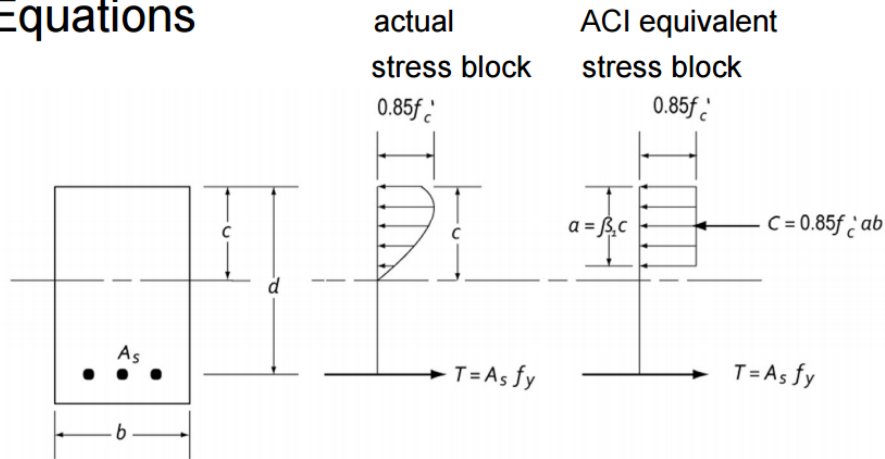


# Analysis of rectangular beam

## Flexure Equations



$$C = T$$

$$0.85f'_c ab = A_s f_y$$

solving for  $a$ ,

$$a = \frac{A_s f_y}{0.85f'_c b} = \frac{\rho f_y d}{0.85f'_c}$$

$$\rho = \frac{A_s}{bd}$$

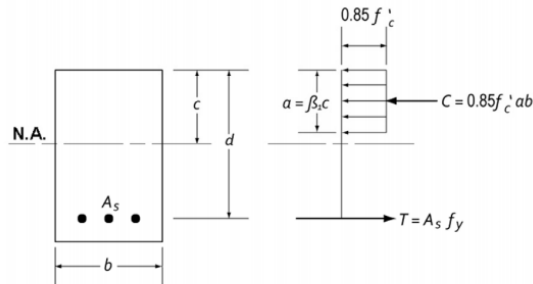
$$M_n = T \left( d - \frac{a}{2} \right) = A_s f_y \left( d - \frac{a}{2} \right)$$

$$M_u = \phi M_n$$

$$M_u = \phi M_n = \phi A_s f_y \left( d - \frac{a}{2} \right)$$

$$M_u = \phi A_s f_y d \left( 1 - 0.59 \frac{\rho f_y}{f'_c} \right)$$

## Rectangular Beam Analysis



2. Find  $a$

3. Find nominal  $M_n$

4. Find required  $M_u$

$$M_u = \phi M_n$$

(using old pre-2005  
 $\phi$  value)

$$a = \frac{A_s f_y}{0.85f'_c b} = \frac{(2.37)(60000)}{0.85(4000)(12)} = 3.49$$

$$M_n = A_s f_y \left( d - \frac{a}{2} \right)$$

$$M_u = \phi A_s f_y \left( d - \frac{a}{2} \right)$$

$$M_u = .9(2.37)(60000) \left( 17.5 - \frac{3.49}{2} \right)$$

$$M_u = 2017000 \text{ in-lb}$$

$$M_u = 168 \text{ ft-k}$$

### Analysis of rectangular beam example (done by mr. Naim hassan )

A simply supported beam of 20" total depth & width 12" , here 72.5 grade steel (500w) is used and compressive strength of concrete is 3 ksi. 3#9 bar is used

Find the moment capacity of the beam.

SOLUTION:

GIVEN  $f_y = 60$  Ksi

$$f'_c = 3 \text{ Ksi}$$

$$h = 20''$$

$$d = 20'' - 2.5'' = 17.5''$$

NOW,  $T = C$

$$A_s f_y = 0.85 f'_c a b$$

$$a = \frac{A_s f_y}{0.85 f'_c b} = \frac{3 \times 1 \times 72.5}{0.85 \times 3 \times 12}$$

$$a = 7.11 \text{ inch}$$

$$M_n = T (d - a/2)$$

$$M_n = A_s f_y (d - a/2)$$

$$M_n = 3 \times 1 \times 72.5 \times (17.5 - \frac{7.11}{2})$$

$$M_n = 253 \text{ K-ft}$$